

Popular Summary

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Chemical Data Assimilation: A Case Study of Solar Occultation Data From the Atlas 1 Mission of the Atmospheric Trace Molecule Spectroscopy Experiment

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Abstract. A key advantage of using data assimilation is the propagation of information from data-rich regions to data-poor regions, which is particularly relevant to the use of solar occultation data such as from ATMOS. For the first time an in depth uncertainty analyses is included in a photochemical model-data intercomparison including observation, representativeness, and theoretical uncertainty. Chemical data assimilation of solar occultation measurements can be used to reconstruct full diurnal cycles and to evaluate their chemical self-consistency. This paper considers as an example the measurements made by the Atmospheric Trace Molecule Spectroscopy Experiment (ATMOS) instrument Atlas-1 during March 1992 for a vertical profile in flow tracking co-ordinates at an equivalent PV latitude of 38°S. ATMOS was chosen because it simultaneously observes several species. This equivalent PV latitude was chosen as it was where ATMOS observed the atmosphere's composition over the largest range of altitudes. A single vertical profile was used so that the detailed diurnal information that assimilation utilizes could be highlighted. There is generally good self-consistency between the ATMOS Atlas-1 observations of O₃, NO, NO₂, N₂O₅, HNO₃, HO₂NO₂, HCN, ClONO₂, HCl, H₂O, CO, CO₂, CH₄, and N₂O, and between the observations and photochemical theory.

1. Introduction

For more than two decades vertical profile measurements of trace gases have been made by solar occultation (e.g. from the Stratospheric Aerosol and Gas Experiment (SAGE), the Halogen Occultation Experiment (HALOE), Polar Ozone and Aerosol Measurement (POAM), the Atmospheric Trace Molecule Spectroscopy Experiment (ATMOS), and the Improved Limb Atmospheric Sounder (ILAS)). The observations are self-calibrating and are therefore useful for the analysis of temporal trends. However, by definition the use of solar occultation limits the measurement opportunities to satellite sunrise and sunset. It is therefore useful to use chemical data assimilation cast in flow tracking co-ordinates to reconstruct full diurnal cycles and to check the chemical self-consistency of the solar occultation measurements. The use of flow-tracking co-ordinates allows a more complete global view to be obtained from the sparse latitudinal coverage of the solar occultation measurements.

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2. Why Use Assimilation?

The question could be asked, 'How does using chemical data assimilation differ from using reverse domain filling (RDF) isentropic trajectories where ozone depletion is computed along trajectories using aircraft and satellite data or other 2D and 3D photochemical models?'

Chemical data assimilation combines the observational information available from measurements with the theoretical information encapsulated into a deterministic model of atmospheric chemistry, together with the associated uncertainties of each. Specifically assimilation uses:

- Constituent observations (in this case observations of 14 constituents *simultaneously*).
- Observational uncertainty.
- Theoretical knowledge to propagate information from the observations available to other species and locations *and* evaluate chemical self consistency.
- Provide an uncertainty on the analysis produced that accounts for observational uncertainty, temporal and spatial representativeness uncertainty, and theoretical (model) uncertainty, i.e. assimilation requires a specification of the error statistics of the observations and the underlying model.

For example, Figure 1 below shows the time evolution of the NO and NO₂ analyses *and* the analyses uncertainty. Conventional modelling studies do not present the time evolution of uncertainty associated with their predictions. Very useful as they are, techniques such as reverse domain filling (RDF) isentropic trajectories, or 2D and 3D chemical models are not able to do this.

Assimilation should not be seen as competing with other modelling tools, rather its purpose is objective improvement by combining observational, theoretical, and uncertainty information formally and statistically in a mathematical framework.

The key aim in developing such a powerful method is to look at scientific issues. However, the credentials of the method must first be rigorously established. The purpose of this paper is to evaluate critically the analyses produced by chemical data assimilation and evaluate its skill with objective measures. Subsequent papers will use the method to look at a variety of scientific issues. For example: The role of halogens in the initiation and catalysis of methane oxidation in the upper troposphere lower stratosphere region. The time evolution and partitioning of nitrogen, chlorine, bromine, and hydrogen species and the relative importance of ozone loss catalytic cycles from the start of the Upper Atmosphere Research Satellite (UARS) period to the present.

2.1. Flow Tracking Coordinates

Under adiabatic conditions air parcels move along isentropic surfaces (surfaces of constant potential temperature, θ). So when considering tracer fields θ is a suitable vertical coordinate. McIntyre and Palmer [1983, 1984], Hoskins *et al.* [1985], and Hoskins [1991] have shown the value of isentropic maps of Ertel's potential vorticity (PV) for visualising large scale dynamical processes. PV plays a central role in large scale dynamics where it behaves as an approximate material tracer [Hoskins *et al.*, 1985].

As a result, PV can be used as the horizontal spatial coordinate instead of latitude and longitude [Norton, 1994; Lary *et al.*, 1995a]. PV is sufficiently monotonic in latitude on an isentropic surface to act as a useful replacement coordinate for both latitude and longitude, reducing the tracer field from three dimensions to two. These ideas have already led to interesting studies correlating PV and chemical tracers such as N_2O and O_3 [Schoeberl *et al.*, 1989; Proffitt *et al.*, 1989, 1993; Lait *et al.*, 1990; Douglass *et al.*, 1990; Proffitt *et al.*, 1989, 1993; Atkinson, 1993]. A key result of these studies is that PV and ozone mixing ratios are correlated on isentropic surfaces in the lower stratosphere, as was first pointed out by Danielsen [1968].

Since the absolute values of PV depend strongly upon height and the meteorological condition, it is useful to normalise PV and use PV equivalent latitude (ϕ_e) as the horizontal coordinate instead of PV itself. ϕ_e is calculated by considering the area enclosed within a given PV contour on a given θ surface. The ϕ_e assigned to every point on this PV contour is the latitude of a latitude circle which encloses the same area as that PV contour. Therefore, for every level in the atmosphere ϕ_e has the same range of values, -90° to 90° . This provides a vortex-tracking, and indeed a flow-tracking, stratospheric coordinate system.

We have taken these now well established ideas and used them as a framework for our chemical data assimilation. This approach is valid for our analysis interval of one day, and often for up to ten days or longer in the stratosphere. Because a major component of the variability of trace gases is due to atmospheric transport it makes sense to use a coordinate system that 'follows' the large scale flow pattern to perform our data assimilation.

3. ATMOS Observations

As an example of how chemical data assimilation cast in flow tracking co-ordinates can be used to extend the value of solar occultation datasets we consider the Atlas-1 data from the Atmospheric Trace Molecule Spectroscopy Experiment (ATMOS) instrument.

ATMOS is an infrared spectrometer (a Fourier transform interferometer) that was designed to study the chemical

composition of the atmosphere. The ATMOS instrument has flown four times on the Space Shuttle, Spacelab-3 in April 1985, and Atlas 1, 2, and 3 in March 1992, April 1993, and November 1994. In this study we use all the data from Atlas 1 for a vertical profile in our flow tracking co-ordinates at an equivalent PV latitude, ϕ_e , of 38°S . This equivalent PV latitude was chosen as it was where ATMOS observed the atmosphere's composition over the largest range of altitudes. We wanted to study a single vertical profile so that the detailed diurnal information that assimilation provides could be highlighted. We assimilated ATMOS Atlas-1 observations of 14 species, namely: O_3 , NO , NO_2 , N_2O_5 , HNO_3 , HO_2NO_2 , HCN , ClONO_2 , HCl , H_2O , CO , CO_2 , CH_4 , and N_2O .

The relative role played by the observations of different species in the assimilation is an interesting issue studied in Lary [submittedb]. Based on the method described in Lary [submittedb] the top ten ranking of chemical information content for this vertical situation over an entire diurnal cycle is O_3 , CO , HO_2 , NO_2 , ClO , CH_3OO , HCHO , NO , BrO , and H_2O . It is not at all surprising, in fact rather reassuring, that O_3 comes out as number one. We also see key representatives of carbon, nitrogen, hydrogen, and bromine species reminding us how coupled atmospheric chemistry is. It is interesting that two of the top ten are peroxy radicals, number three is HO_2 and number six is CH_3OO . It is also noteworthy that the methyl species are rarely considered in stratospheric studies yet have significant information content.

4. Chemical Assimilation Scheme

Data assimilation enables better use of observations of atmospheric chemistry. An example of the way assimilation can reconstruct a full diurnal cycle from occultation observations is shown in Figure 1. This example will be discussed more later.

The first use of chemical data assimilation was by Fisher and Lary [1995]. Khattatov *et al.* [1999] have described the chemical Kalman filter used in this study. Other studies using assimilation include Elbern [1997]; Elbern *et al.* [1997]; Eskes *et al.* [1998, 1999]; Khattatov *et al.* [1999]; Lary [1999]; Elbern *et al.* [2000]; Khattatov *et al.* [2000, 2001]; Wang *et al.* [2001]; Smyshlyaev and Geller [2001]; Clerbaux *et al.* [2001]; Errera and Fonteyn [2002]; Chipperfield *et al.* [2002]; Daescu and Carmichael [2003]. The photochemical mode used is the extensively validated AutoChem model [Fisher and Lary, 1995; Lary *et al.*, 1995b; Lary, 1996]. The model is explicit and uses an adaptive-timestep, error monitoring time integration scheme for stiff systems of equations [Press *et al.*, 1992; Stoer and Bulirsch, 1980]. AutoChem was the first model to perform 4D variational data assimilation (4D-VAR) Fisher and Lary [1995] and now also includes a Kalman filter Khattatov *et al.* [1999]. AutoChem uses kinetic data largely based on Atkinson *et al.* [1997]; DeMore *et al.* [1997] with updates for nitrogen chemistry based on Brown *et al.* [1999a]; Portmann *et al.* [1999]; Brown *et al.* [1999b].

A key part of the chemical model is the calculation of photolysis rates. In this study they are calculated using full spherical geometry and multiple scattering [Anderson, 1983; Lary and Pyle, 1991a, b; Meier *et al.*, 1982; Nicolet

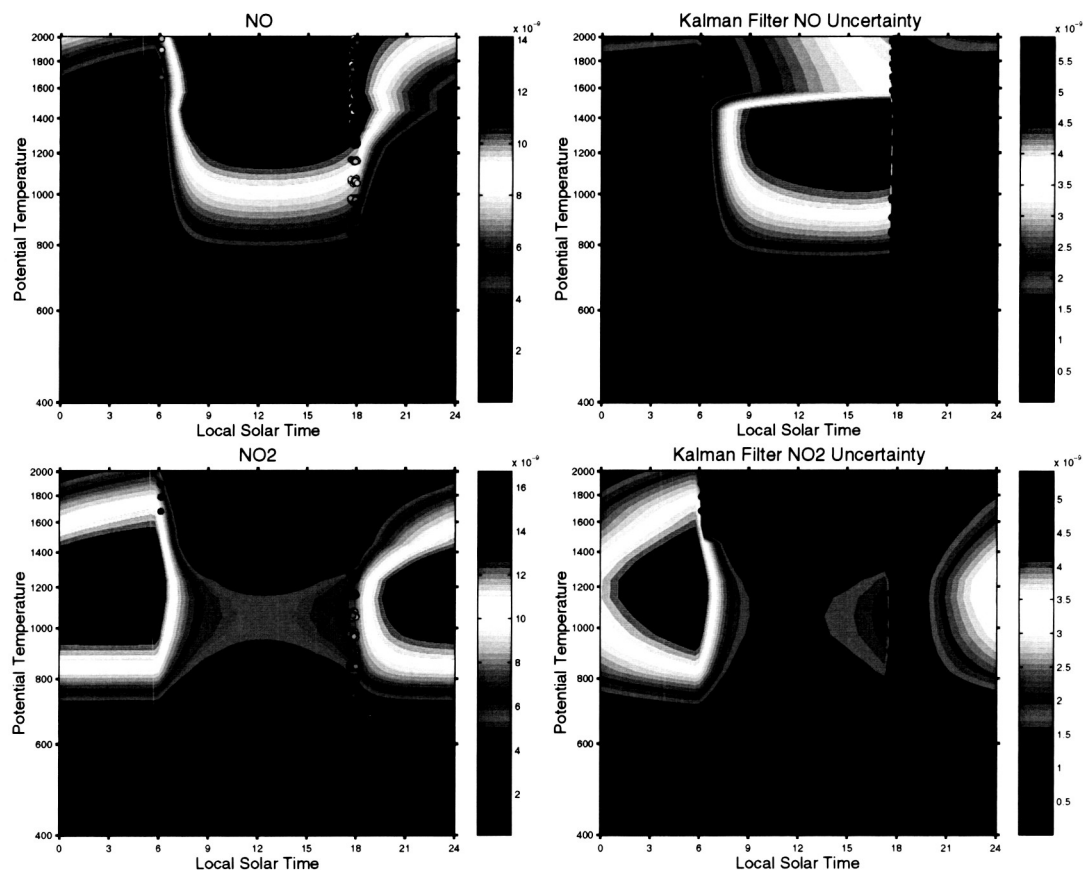


Figure 1. Diurnal cycles of NO, and NO₂ vertical profiles for the 30 March 1992 assimilation of ATMOS Atlas-1 data at 38°S. The left hand panel show the chemical analyses produced by assimilation overlaid with the observations (color filled circles). The right hand panel show the analyses uncertainties overlaid with the observation uncertainties (color filled circles). The reduction in analyses uncertainty can be seen in the right hand plots when new observational information comes in. The dots indicate the locations of the assimilation analyses grid. A single vertical profile was used so that the detailed diurnal information that assimilation utilizes could be highlighted.

et al., 1982] corrected after *Becker et al.* [2000]. The photolysis rate used for each time step is obtained by ten point Gaussian-Legendre integration [*Press et al.*, 1992]. These calculations are updated on every assimilation iteration to ensure that the improved ozone profile at a given equivalent latitude is used to calculate the photolysis rates.

The chemical system under study here contains a total of 60 species. 55 species are time integrated, namely: O(¹D), O(³P), O₃, N, NO, NO₂, NO₃, N₂O₅, HONO, HNO₃, HO₂NO₂, CN, NCO, HCN, Cl, Cl₂, ClO, ClOO, OClO, Cl₂O₂, ClONO₂, ClONO, ClONO₂, HCl, HOCl, CH₃OCl, Br, Br₂, BrO, BrONO₂, BrONO, HBr, HOBr, BrCl, H₂, H, OH, HO₂, H₂O₂, CH₃, CH₃O, CH₃O₂, CH₃OH, CH₃OOH, CH₃ONO₂, CH₃O₂NO₂, HCO, HCHO, CH₄, CH₃Br, CF₂Cl₂, CO, N₂O, CO₂, H₂O. The remaining 5 species are not integrated and are not in photochemical equilibrium, namely: O₂, N₂, HCl(s), H₂O(s), HNO₃(s). The model contains a total of 420 reactions, 278 bimolecular reactions, 32 trimolecular reactions, 60 photolysis reactions, 4 cosmic ray processes, and 46 heterogeneous reactions.

The first guess used came from a January simulation of the Cambridge 2D chemical model [*Law and Pyle*, 1991, 1993a, b]. As these are not particularly well suited to

the conditions observed by ATMOS during March 1992 our chemical assimilation was cycled three times. The results presented are from the third cycle. This allowed for quite rapid convergence to the conditions observed by ATMOS. Each cycle involves a first guess simulation, followed by two iterations of the chemical Kalman filter, and then an analysis simulation. The analysis simulation is a free running chemical simulation starting from the chemical state vector at the end of the chemical Kalman filter. This is done to mimic the way 4D-variational data assimilation works with the added advantage of having the time evolution of the full species error co-variance matrix. This is desirable as it means there are no steps in the species concentrations with time due to Kalman filter increments (i.e. no time discontinuities when new information is used).

4.1. Observations

The key difference between conventional modelling and data assimilation is the use of observations and information on observational and other uncertainties. The uncertainties we consider are the observational uncertainty quoted by the observation team, the representativeness uncertainty (i.e. the spatial variability over an analysis grid cell) and the photochemical theoretical uncertainty.

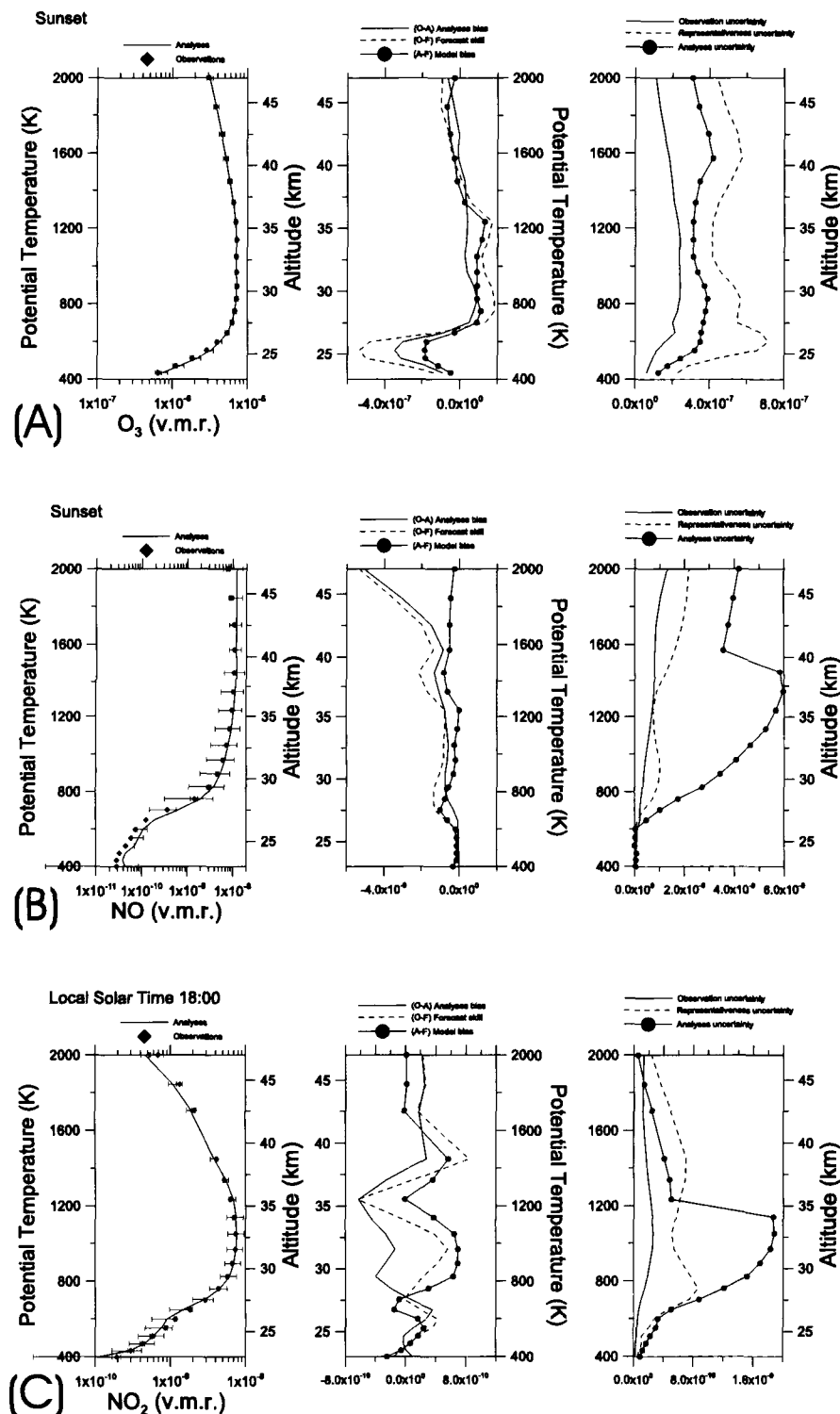


Figure 2. Vertical profiles for O_3 , NO , and NO_2 of analyses and observations (left panel). The middle panel shows the skill measures described in §4.4, namely the observation increment (O-F) which is a measure of forecast skill, the analysis increment (A-F) which is a measure of model bias, and the analysis-observations (A-O) which is a measure of the analyses bias. The right hand panel shows the uncertainties, observational, representativeness, and analyses. All panels are from the 30 March 1992 assimilation of ATMOS Atlas-1 data at 38°S. Observations and observation error bars in blue.

We obtain information on the representativeness uncertainty and improve the signal to noise by using all observations available within a grid cell and studying the probability distribution function (PDF) of these observations. The width of the PDF is used as a measure of the variability or representativeness uncertainty for the grid cell. When more than one observation is available in a grid cell we take the median of the PDF as the observation for that cell, and the median of the observation uncertainty PDF as the observation uncertainty for that grid cell. So both the observation and observation uncertainty are obtained directly from the data in a way that they are truly representative of that grid cell.

The Kalman filter assimilation is a multivariate technique which can simultaneously process observation/uncertainty information pairs of the 55 time integrated species, whenever and wherever they are available, together with the theoretical information from our photochemical model.

4.1.1. Temporal Search Criteria.

The criteria used to determine at what time we use an observation are local solar time and solar zenith angle. In the case of short lived species, or those with a significant diurnal cycle, such as NO and NO₂, the observation solar zenith angle needs to be within 2° of the analyses time step solar zenith angle, and also the observation local solar time needs to be within one hour of the analyses local solar time, for the observation to be used. This ensures that sunrise measurements are used at sunrise, and that sunset measurements are used at sunset. This is also important as there can be a significant difference between the geographic latitude and the equivalent PV latitude. As our analysis grid uses equivalent PV latitude it is important that we use the local solar zenith angle as the criteria for using an observation, and not just the local solar time. In the case of longer lived species, or those without a significant diurnal cycle, we can use less stringent criteria. For these longer lived species we specify that the observation solar zenith angle needs to be within 6° of the analyses time step solar zenith angle, and also the observation local solar time needs to be within one hour of the analyses local solar time. These in fact are rather strict criteria for the long lived species. Sensitivity experiments have shown that much more lax values work just as well for the long lived species.

4.1.2. Spatial Search Criteria.

The criteria used to determine at what location we use an observation are equivalent PV latitude (ϕ_e), and potential temperature (θ). An observation is used in ϕ_e - θ grid box where it lies. The grid has 21 potential temperature levels spaced equally in $\log(\theta)$ between 400 K and 2000 K, and 32 equivalent PV latitudes spaced evenly between -90° and 90°. That means that no interaction between the boxes (meridional transport, mixing, diabatic ascent/descent) is considered.

We have chosen to deal with a vertical profile of observations at a time as vertical profiles can contain gaps. These are easy to fill in by eye, but for an algorithm to deal with the data voids we need to consider an entire profile at a time in our flow tracking co-ordinate space. In a full 3D assimilation the 3D spatial co-variance matrix would be performing this task. However, in this study we are using an array of 0D boxes with a full Kalman filter and detailed chemistry. To make this computationally achievable we use multiple 0D box models which are stacked into a series of profiles.

Which gives us a 2D global assimilation with 21 potential temperature levels spaced equally in $\log(\theta)$ between 400 K and 2000 K, and 32 equivalent PV latitudes spaced evenly between -90° and 90°.

So to clarify, the actual assimilation is done in a 2D array of completely independent boxes. However, the observation reconstructions used for this independent array of boxes are generated considering an entire profile at a time, where the profile is a function of potential temperature for a given equivalent PV latitude range. The equivalent PV latitude range is the width of the grid box. This is not ideal, but is a necessary and good approximation because of the computer time required to do a full 3D assimilation with a Kalman filter.

Our observation reconstruction algorithm consists of the following steps:

1. For each level in the analyses profile we determine which observations lie between the bottom of the level below and the top of the level above.
2. If there are more than n_{thresh} (usually taken to be 25) observations we sort them in order of their percentage uncertainty and just use the n_{thresh} most reliable data points (i.e. those with the lowest concentration uncertainty to concentration ratio).
3. For these data points we calculate the median concentration.
4. If there are any levels which have no observations bracketed above and below by levels which did have observations we linearly interpolate using the available values above and below.

4.2. Observation Uncertainties

The uncertainty of the reconstructed observation has two components. First, for each (ϕ_e, θ) grid box we have a distribution of observed concentrations, and a distribution of observed concentration uncertainties. We take the observational uncertainty to be the median observed concentration uncertainty for the current distribution in the given (ϕ_e, θ) grid box. Second, the representativeness uncertainty. Information on the representativeness uncertainty is gained by using all observations available within a grid cell and studying the probability distribution function (PDF) of these observations. The width of the PDF is used as a measure of the variability or representativeness uncertainty for the (ϕ_e, θ) grid cell. So both the observation and observation uncertainty used are directly from the data but selected in a way that we are sure they are truly representative of that grid cell. The average deviation, or mean absolute deviation, is a robust estimator of the width of the distribution [Press *et al.*, 1992].

$$\sigma_{rep} = ADev(\chi_1 \dots \chi_N) = \frac{1}{N} \sum_{j=1}^N |\chi_j - \bar{\chi}| \quad (1)$$

Where χ_j refers to the individual concentration observations available in the grid cell. The reconstructed observation for the (ϕ_e, θ) grid box is the median of the 25 most accurate observations available in the grid box. The median is used so that the reconstructed observations, and hence the analyses, are not affected by outliers.

Lary [submitted] show that the representativeness uncertainty is an interesting quantity as it clearly picks out mixing barriers such as the polar vortices, the tropical pipe, and the tropopause. In addition, for species such as ozone

in polar day we see a large representativeness uncertainty at the summer pole. It is important to note that this representativeness uncertainty is fully accounted for and goes in to the analyses and is reflected in the analyses uncertainty.

Whatever co-ordinate system is used such situations will be encountered, it is therefore important to account for the grid representativeness uncertainty as accurately as possible and include them in the analyses.

It is also fair to observe that this level of treatment of uncertainties is seldom, if ever, performed for atmospheric chemical modeling. It is suggested that this is a major step taken in this study.

4.3. Photochemical Theory Uncertainties

Currently we assume a growth rate in the photochemical theory uncertainty of 5% per time step (i.e. the diagonal of the co-variance matrix is increased by 5% at each time step to crudely account for photochemical theory uncertainties). The time step used here is 15 minutes, but we often use a one hour time step also. This is deliberately conservative to avoid filter divergence. In future we want to explicitly calculate the photochemical theory uncertainty by using the uncertainty in each rate coefficient and the constituent concentrations.

4.4. Analyses Quality Measures

Once the analyses has been performed we quantify their quality by generating a set of statistics that compare the observations used in making the analyses with the analyses itself.

1. **Observation Increment, (O-F).** This typically is the best measure of forecast skill. The difference between the first guess and the observations, also known as observed-minus-background differences or the innovation vector [Daley, 1991].

$$(O - F) = \frac{1}{n} \sum_{k=1}^n (o_k - f_k) \quad (2)$$

where o_k denotes the k th observation and f_k the corresponding value from the first guess forecast. The lower the absolute value of (O-F) the better.

2. **Analysis Increment, (A-F).** This is a good measure of model bias. The difference between the first guess and the final analyses, also known as analysis-minus-background differences or the correction vector [Daley, 1991].

$$(A - F) = \frac{1}{n} \sum_{k=1}^n (a_k - f_k) \quad (3)$$

where a_k denotes the analyses and f_k the corresponding value from the first guess forecast. The lower the absolute value of (A-F) the better.

3. **Analysis-Observations (A-O).** This typically is the best measure of the analyses bias. The difference between the analyses and the observations, also known as analysis-minus-observed differences or the innovation vector [Daley, 1991].

$$(A - O) = \frac{1}{n} \sum_{k=1}^n (a_k - o_k) \quad (4)$$

where o_k denotes the k th observation and a_k the corresponding value from the analyses. The lower the absolute value of (A-O) the better.

5. Assessment of the Assimilation

ATMOS Atlas-1 observed 14 of the 55 species our assimilation scheme can simultaneously analyze. These 14 observed species include key species in reactive nitrogen and chlorine chemistry as well as several long lived source gases. The Atlas-1 observations are only available at satellite sunrise and sunset. In this case study for 30 March 1992 the measurements are mainly available at sunset.

5.1. O₃

Figure 2 (a) displays vertical profiles for the 30 March 1992 assimilation (ATMOS Atlas-1) of the O₃ analyses concentrations, uncertainties, and skill measures. The left hand panel shows that there is excellent agreement between the ATMOS observations (diamonds with error bars) and the analyses (line with error bars).

The total observational uncertainty has two components, the measurement uncertainty (solid line in the right hand panel) and the representativeness uncertainty (dashed line). The representativeness uncertainty attempts to quantify the spatial variability of ozone over the grid box. This has been quantified by using the average deviation of observed in each grid box. The analyses uncertainty is the diagonal element of the time integrated Kalman filter error co-variance matrix (solid line with overlaid circles). It can be seen that these uncertainties are of the order of 0.1 ppmv, or a few percent.

The analyses bias, (O-A), is small and well within the observational uncertainties. The Forecast skill, (O-F), and model bias (A-F), are a little larger. This is because the apriori first guess was not entirely suitable for the situation ATMOS observed. As was mentioned in the introduction it came from a 2D model of the atmosphere.

5.2. NO and NO₂

Full diurnal cycles produced by the assimilation for NO and NO₂ from the occultation measurements are shown in Figure 1. The left hand plots show the analyses overlaid with the observations (color filled triangles). The right hand plots show the analyses uncertainties overlaid with the observation uncertainties (color filled triangles). The reduction in analyses uncertainty can be seen in the right hand plots when new observational information comes in. The dots indicate the locations of the assimilation analyses grid.

Figure 2 (b) and (c) display vertical slices through the NO and NO₂ diurnal cycles at sunset. The left hand panels of Figure 2 (b) and (c) shows that there is good agreement between the ATMOS observations (diamonds with error bars) and the analyses (line with error bars).

5.3. N₂O₅, HNO₃, and HO₂NO₂

Figure 3 (a) to (c) display vertical slices through the N₂O₅, HNO₃, and HO₂NO₂ diurnal cycles at sunset. For each of these species the analyses and observations agree to within the analyses uncertainty.

5.4. Other Species

Figure 4 displays vertical slices through the ClONO₂, HCl, HCN, NO₂, CH₄, H₂O, CO and CO₂ diurnal cycles at sunset. For each of these species the analyses and observations agree to within the analyses uncertainty. It is noteworthy that in some cases (for example ClONO₂) the assimilation gives a larger uncertainty than was specified by the measurement team. This occurs for at least two reasons:

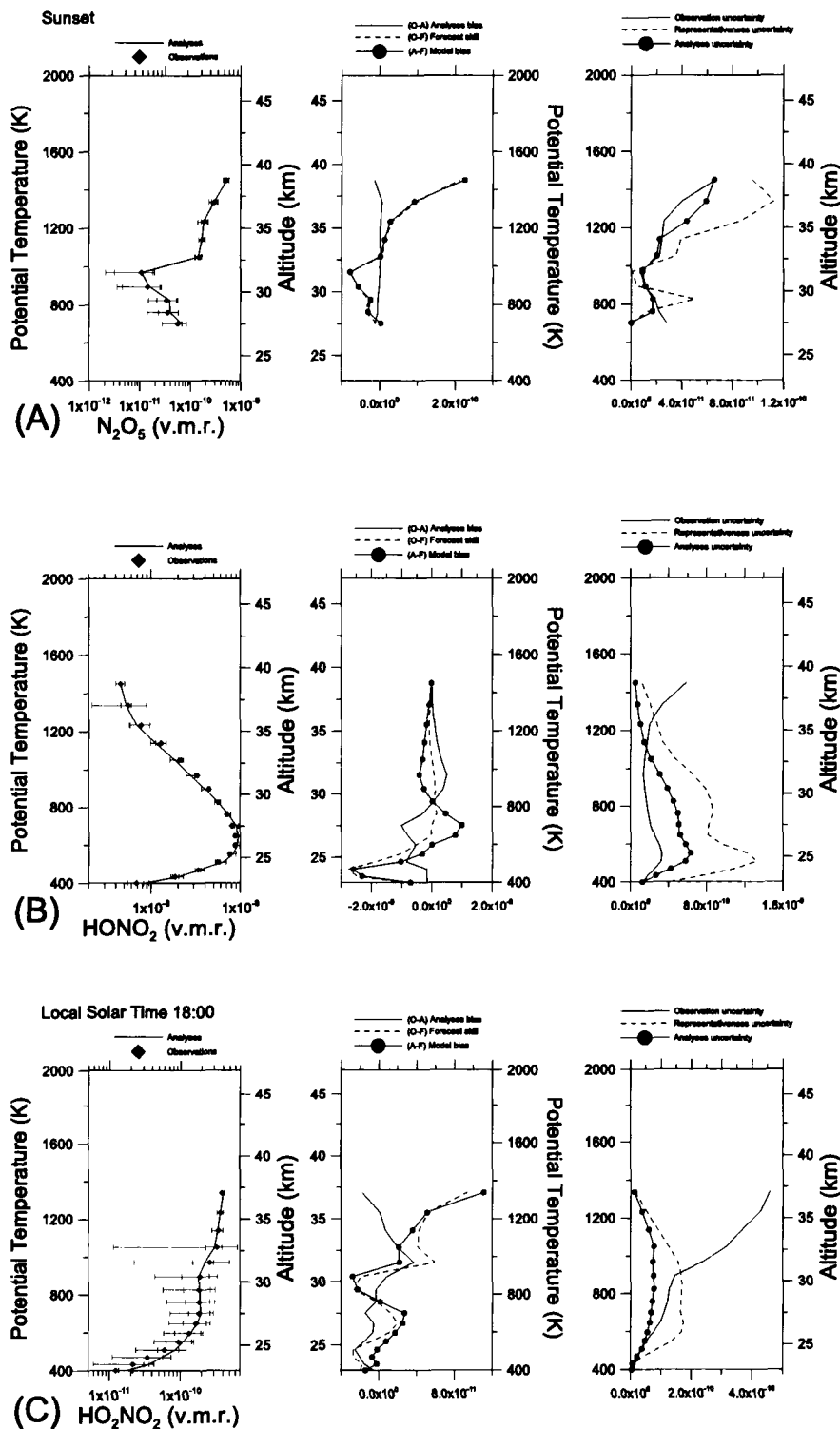


Figure 3. Vertical profiles for N_2O_5 , HONO_2 , and HO_2NO_2 of analyses and observations (left panel). The middle panel shows the skill measures described in §4.4, namely the observation increment (O-F) which is a measure of forecast skill, the analysis increment (A-F) which is a measure of model bias, and the analysis-observations (A-O) which is a measure of the analyses bias. The right hand panel shows the uncertainties, observational, representativeness, and analyses. All panels are from the 30 March 1992 assimilation of ATMOS Atlas-1 data at 38°S . Observations and observation error bars in blue.

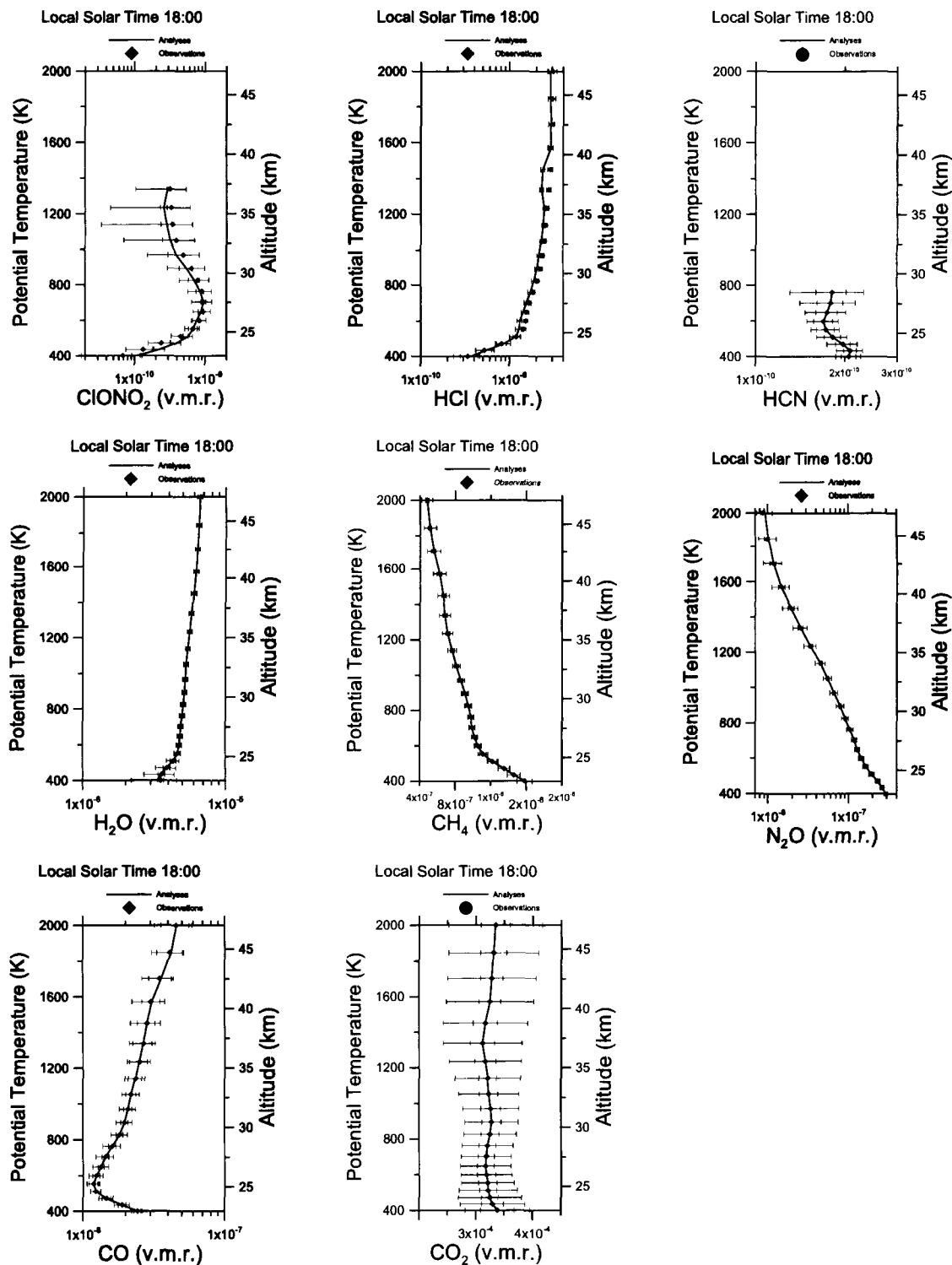


Figure 4. Vertical profiles for ClONO₂, HCl, HCN, NO₂, CH₄, H₂O, CO and CO₂ analyses from the 30 March 1992 assimilation of ATMOS Atlas-1 data at 38°S. Observations and observation error bars in blue.

1. The assimilation also accounts for the representativeness uncertainty. In some cases where there are large spatial gradients this uncertainty can be larger, even considerably larger, than the observational uncertainty. The analyses uncertainty reflects this as well as the photochemical model uncertainty.

2. Information on this species is propagating through the assimilation system from observations of other chemically coupled species. This other information with its associated weight (uncertainty) is not entirely consistent with the observations and so the analyses acquires a higher uncertainty, for example due to the presence of observation or model biases.

6. Data-Theory Intercomparison

A key advantage of using data assimilation is the propagation of information from data-rich regions to data-poor regions, which is very relevant to the assimilation of solar occultation data such as from ATMOS.

6.1. Mathematical Framework For Intercomparison

Previous studies, such as *Chang et al.* [1996], have shown good agreement of volume mixing ratio profiles measured by ATMOS with in situ measurements acquired from platforms on the NASA ER-2. *Sen et al.* [1998] presented volume mixing ratio profiles of NO, NO₂, HONO, HO₂NO₂, N₂O₅, and ClONO₂ and their composite budget (NO_y), from 20 to 39 km, measured remotely in solar occultation by the Jet Propulsion Laboratory MkIV Interferometer during a balloon flight from Fort Sumner, New Mexico (35°N), on September 25, 1993. In general, the observed profiles agree well with values calculated using a photochemical steady state model constrained by simultaneous MkIV observations of long-lived precursors and aerosol surface area from the Stratospheric Aerosol and Gas Experiment II.

What is new in this study is that the comparison between observations and photochemical theory, and the constraint of photochemical theory by observations is done within an objective mathematical framework where full account is taken of information uncertainty both in the observations and photochemical theory. Previous ATMOS intercomparisons have not done this.

After examining the figures in this paper it may be asked, 'How much information is ATMOS providing, and how is this any different from what we would obtain from using a free running model?' ATMOS has provided a great deal of information for the figures shown here. If it was not for the constraint of ATMOS Atlas-1 observations the sunset observations would *not* have agreed with the photochemical model, and not simultaneously agreed with the O₃, NO, NO₂, N₂O₅, HNO₃, HO₂NO₂, HCN, ClONO₂, HCl, H₂O, CO, CO₂, CH₄, and N₂O.

6.2. Quantifying Uncertainty

If the primary interest is the likely magnitude of diurnal variation then one does NOT need assimilation. The reason for using the assimilation is to *simultaneously* use as much information as we have and to provide an estimate of the uncertainty associated with this information which includes a treatment of observational uncertainty, spatial and temporal representativeness uncertainty, and photochemical theory uncertainty. Assimilation also allows objective self-consistency tests such as those described in §4.4, and the χ^2 test of (O-F) proposed by *Dee* [1995], applied by *Menard*

et al. [2000]; *Menard and Chang* [2000], and *Khattatov et al.* [2000]. The currently available techniques other than assimilation do not provide this capability.

6.3. Inferring Information on Unobserved Quantities

In the case of a quality dataset, such as ATMOS, the assimilation can reliably produce full diurnal cycles from just occultation observations, and relatively reliably infer analyses for unobserved species. In this case study full diurnal analyses and uncertainties of 55 species were produced from observations of just 14 of these species. In addition the assimilation has provided a useful check for photochemical self-consistency between the ATMOS observations, and between the observations and photochemical theory. Self-consistency is not always present between the multi constituent observations made from a given platform, for example UARS observed NO₂ from three instruments which were not self-consistent with each other. This will be the subject of further papers.

The reason for choosing 38°S for this case study is that at this latitude there was the greatest vertical extent of ATMOS Atlas-1 observations. The good agreement obtained between ATMOS observations and photochemical theory reported here was not the result of a fortuitous choice of data. Many other studies have been performed with data from numerous platforms including other ATMOS missions, MkIV balloon flights, ER-2 data, and UARS data. Space does not allow to present these here, they will be the subject of other papers.

Observations from other platforms and measurement campaigns have been considered, such as the Stratospheric Photochemistry Aerosol and Dynamics Experiment (SPADE) in May 1993 and the Cryogenic Limb Array Etalon Spectrometer (CLAES), which have much more diurnal coverage than just sunrise and sunset and show the same result. Chemical data assimilation can reconstruct well an entire diurnal cycle from reliable observations at one time. Whether the observations are at sunrise, sunset or spaced throughout the day.

This means that multispecies chemical data assimilation is likely to be useful for data product monitoring and quality assessment. This is relevant to the use of data assimilation within a validation campaign of new instruments such as those to be placed on board EOS AURA. Solar occultation data (such as from the Canadian Atmospheric Chemistry Experiment, ACE, and HALOE), aircraft data (such as from the DC-8 and ER-2) and balloon data (such as the MkIV) could be used to reconstruct full-diurnal cycles of species such as NO and NO₂, thus relaxing the local solar time/zenith angle coincidence requirements needed to validate AURA observations.

7. Summary

Multispecies chemical data assimilation is useful for constituent data product monitoring/validation and quality assessment. Two key advantages of using data assimilation is the ability to check the chemical self-consistency of multispecies observations and information prorogating from data-rich regions to data-poor regions. This is particularly relevant to the assimilation of solar occultation data such as from ATMOS.

Chemical data assimilation has been able to take solar occultation measurements of 14 species at sunrise and sunset and produce full diurnal cycles for 55 observed and unobserved species together with their associated uncertainty. The associated uncertainty includes a treatment of the observation, representativeness, and photochemical theory uncertainty.

We confirm that there is self-consistency between the ATMOS Atlas-1 observations of O_3 , NO , NO_2 , N_2O_5 , HNO_3 , HO_2NO_2 , HCN , $ClONO_2$, HCl , H_2O , CO , CO_2 , CH_4 , and N_2O , and between ATMOS and photochemical theory. If there had been inconsistency between the observations and photochemical theory the assimilation skill scores such as (O-F), and (O-A) would have highlighted these and quantified their magnitude.

Future studies in preparation using chemical data assimilation include those to look at: The halogen catalyzed oxidation of hydrocarbons in the upper troposphere and lower stratosphere. The partitioning of hydrogen, nitrogen, chlorine, bromine, and carbon species as a function of temperature, solar illumination and aerosol loading. The relative roles of catalytic ozone loss cycles and how they have changed with time and location over the UARS period. Satellite instrument validation including Envisat, ACE, and AURA.

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